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## $\mathrm{K}_{6}\left[\mathrm{As}_{\mathbf{6}} \mathbf{V}_{\mathbf{1 5}} \mathbf{O}_{\mathbf{4 2}}\left(\mathbf{H}_{\mathbf{2}} \mathbf{O}\right)\right] . \mathbf{6 H}_{\mathbf{2}} \mathbf{O}$

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## Abstract

The crystal structure of hexapotassium dotetracontaoxo(hexaarsenio)pentadecavanadate(IV) heptahydrate, $\mathrm{K}_{6}$ [ $\left.\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] .6 \mathrm{H}_{2} \mathrm{O}$, is composed of an $\left[\mathrm{As}_{6} \mathrm{~V}_{15}-\right.$ $\left.\mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{6-}$ anion, which has $D_{3}$ symmetry, and six seven-coordinate potassium ions. There is an $\mathrm{H}_{2} \mathrm{O}$ molecule at the centre of the heteropolyanion. This anion consists of $\mathrm{VO}_{5}$ pyramids linked by $\mathrm{As}_{2} \mathrm{O}_{5}$ units through shared O atoms. The $\mathrm{V}-\mathrm{O}$ distances range from 1.604 (4) to 2.009 (4) $\AA$, As-O from 1.772 (4) to 1.793 (3) $\AA$, and $\mathrm{K} \cdots \mathrm{O}$ from 2.676 (6) to 3.311 (4) Å.

## Comment

Iso- and heteropolyvanadates usually contain molecular anions with interesting cage structures. These polyvanadate cage anions form inclusion compounds with neutral molecules and anions, among which are [ $\mathrm{V}_{12}-$ $\left.\mathrm{O}_{32}(\mathrm{MeCN})\right]^{4-}$ (Day et al., 1989), $\left[\mathrm{V}_{18} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{12^{-}}$ (Johnson \& Schlemper, 1978), $\left[\mathrm{V}_{18} \mathrm{O}_{42} \mathrm{H}_{9}\left(\mathrm{VO}_{4}\right)\right]^{6-}$, $\left[\mathrm{V}_{18} \mathrm{O}_{42}\left(\mathrm{SO}_{4}\right)\right]^{8-},\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{6-},\left[\mathrm{As}_{8} \mathrm{~V}_{1+} \mathrm{O}_{42}-\right.$ $\left.\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{4-},\left[\mathrm{As}_{8} \mathrm{~V}_{14} \mathrm{O}_{42}(X)\right]^{6-}\left(X=\mathrm{SO}_{3}^{2-}\right.$ or $\mathrm{SO}_{4}^{2^{2-}}$; Müller \& Döring, 1991) and $\left[\mathrm{As}_{8} \mathrm{~V}_{14} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)_{1 / 2}\right]^{4-}$ (Huan et al., 1991). The crystal structure has been reported for an $\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{6-}$ anion with $\mathrm{H}_{2} \mathrm{O}$ at the centre in $\mathrm{K}_{6}\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] .8 \mathrm{H}_{2} \mathrm{O}$ (Müller \& Döring, 1988, 1991). The present study concerns the phase $\mathrm{K}_{6}\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] .6 \mathrm{H}_{2} \mathrm{O}$, (I), which contains a similar anion to that found in $\mathrm{K}_{6}\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]$.$8 \mathrm{H}_{2} \mathrm{O}$ (Müller \& Döring, 1988, 1991).


The $\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{6-}$ anion has $D_{3}$ symmetry, and consists of 15 distorted $\mathrm{VO}_{5}$ square pyramids and $\operatorname{six} \mathrm{AsO}_{3}$ triangular pyramids, with a statistically disordered $\mathrm{H}_{2} \mathrm{O}$ molecule at its centre. Two $\mathrm{AsO}_{3}$ groups are joined to each other via an oxygen bridge and form an $\mathrm{As}_{2} \mathrm{O}_{5}$ unit. Every $\mathrm{VO}_{5}$ consists of one terminal O and four bridging O atoms. The $\mathrm{VO}_{5}$ pyramids are joined through vertices and edges to their neighbouring $\mathrm{VO}_{5}$ pyramids, but the $\mathrm{AsO}_{3}$ groups are connected by $\mathrm{VO}_{5}$ pyramids only through vertices. The $15 \mathrm{VO}_{5}$ pyramids linked with one another through vertices and edges are connected by $\mathrm{As}_{2} \mathrm{O}_{5}$ units through shared O atoms, and form a ball-like structure.


Fig. 1. View of the $\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right]^{6-}$ anion, with displacement ellipsoids at the $50 \%$ probability level.

In the crystal lattice, the $\mathrm{VO}_{5}$ pyramids can be divided into three different types. The first V site (V1, V1A, $\mathrm{V} 1 B$ ) contains three $\mathrm{VO}_{5}$ pyramids, which are joined to four $\mathrm{VO}_{5}$ and two $\mathrm{As}_{2} \mathrm{O}_{5}$ units. The second V site includes six $\mathrm{VO}_{5}$ pyramids, each of which is joined to its neighbouring five $\mathrm{VO}_{5}$ pyramids and one $\mathrm{AsO}_{3}$ group. Finally, the third V site contains six $\mathrm{VO}_{5}$ pyramids, which are joined through three $\mathrm{VO}_{5}$ pyramids and two $\mathrm{AsO}_{3}$ groups.

The anions are linked by hydrated potassium ions, which themselves have a distorted sevenfold coordination sphere composed of one bridging and four terminal O atoms from the anions, and two O atoms from the water molecules. Within the anion, a V atom is bound to one terminal O atom at distances of 1.604 (4)1.615 (6) $\AA$ and one $O$ atom shared with two other V atoms, at distances of $1.910(4)-1.955$ (4) $\AA$. The $\mathrm{K} \cdots \mathrm{O}$ and As-O distances are 2.676(6)-3.311 (4) and 1.772 (4)-1.793 (3) $\AA$, respectively. The $\mathrm{V} \ldots \mathrm{V}$ distances are in the range 2.8758 (15)-3.0592 (15) $\AA$. These distances are comparable to those found in similar structures (Müller \& Döring, 1988, 1991). The largest difference between $\mathrm{K}_{6}\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$ and $\mathrm{K}_{6}\left[\mathrm{As}_{6}-\right.$ $\left.\mathrm{V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] .8 \mathrm{H}_{2} \mathrm{O}$ is cell type: the former is a hexagonal cell and the latter is rhombohedral. In both structures, the anion has $D_{3}$ symmetry.

## Experimental

The synthesis of the title compound was carried out by hydrothermal reaction of $\mathrm{H}_{2} \mathrm{O}, \mathrm{V}_{2} \mathrm{O}_{5}, \mathrm{As}_{2} \mathrm{O}_{3}, \mathrm{H}_{3} \mathrm{PO}_{3}$ (25\%), $\mathrm{H}_{2} \mathrm{NCH}_{2} \mathrm{CH}_{2} \mathrm{NH}_{2}$ and KOH (molar ratio 800:6:6:20:6:12) in a 30 ml Teflon-lined stainless steel autoclave for 3 d at 433 K . The dark-green crystals were isolated from the solution once it had been cooled to room temperature.

## Crystal data

$\mathrm{K}_{6}\left[\mathrm{As}_{6} \mathrm{~V}_{15} \mathrm{O}_{42}\left(\mathrm{H}_{2} \mathrm{O}\right)\right] \cdot 6 \mathrm{H}_{2} \mathrm{O}$
$M_{r}=2246.33$
Trigonal
$R \overline{3} c$

$$
\begin{aligned}
& a=17.942(3) \AA \\
& c=28.450(6) \AA \\
& V=7932(2) \AA^{3} \\
& Z=6 \\
& D_{x}=2.822 \mathrm{Mg} \mathrm{~m}^{-3} \\
& D_{m} \text { not measured }
\end{aligned}
$$

Mo $K \alpha$ radiation
$\lambda=0.71073 \AA$
Cell parameters from 30 reflections
$\theta=4.99-12.48^{\circ}$
$\mu=6.825 \mathrm{~mm}^{-1}$
$T=293$ (2) K
Polyhedron
$0.52 \times 0.36 \times 0.24 \mathrm{~mm}$
Dark green

## Data collection

Siemens $P 4$ diffractometer

## $\omega / 2 \theta$ scans

Absorption correction: empirical via $\psi$ scans (North et al., 1968)
$T_{\text {min }}=0.098, T_{\text {max }}=0.194$
3480 measured reflections
1395 independent reflections 1105 reflections with

$$
I>2 \sigma(I)
$$

## Refinement

Refinement on $F^{2}$
$\Delta \rho_{\text {max }}=1.069 \mathrm{e} \mathrm{A}^{-3}$
$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.031$
$w R\left(F^{2}\right)=0.088$
$S=1.143$
1392 reflections
118 parameters
H atoms not located
$w=1 /\left[\sigma^{2}\left(F_{o}^{2}\right)+(0.0377 P)^{2}\right]$
where $P=\left(F_{o}^{2}+2 F_{c}^{2}\right) / 3$
$(\Delta / \sigma)_{\max }<0.001$
$\begin{aligned} & \Delta \rho_{\text {max }}=1.069 \mathrm{e} \AA \AA^{-3} \\ & \Delta \rho_{\text {min }}\end{aligned}=-0.529 \mathrm{~A}^{-3}$
Extinction correction:
SHELXL93 (Sheldrick, 1993)

Extinction coefficient: 0.00015 (2)

Scattering factors from International Tables for Crystallography (Vol. C)

Table 1. Fractional atomic coordinates and equivalent isotropic displacement parameters ( $\AA^{2}$ )

| $U_{\text {eq }}=(1 / 3) \Sigma_{i} \Sigma_{j} U^{i j} a^{\prime} \alpha^{j} \mathbf{a}_{i} \cdot \mathbf{a j}_{j}$. |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
|  | ${ }^{x}$ | ${ }^{y}$ | $z$ | $U_{\text {eq }}$ |
| Asi | 0.46372 (4) | 0.41868 (4) | 0.04994 (2) | 0.0213 (2) |
| V1 | $2 / 3$ | 0.55562 (8) | 1/12 | 0.0193 (4) |
| V2 | 0.60754 (7) | 0.41094 (6) | -0.02096 (3) | $0.0180(3)$ |
| V3 | 0.77689 (7) | 0.54205 (7) | 0.00742 (3) | 0.0190 (3) |
| K | 0.96522 (12) | 0.77970 (11) | -0.05348 (6) | 0.0486 (5) |
| 01 | (0.8223 (3) | 0.6205 (3) | -0.02903 (15) | 0.0217 (12) |
| 02 | 0.5805 (3) | 0.4387 (3) | -0.06872 (14) | 0.0273 (10) |
| 03 | 0.6595 (3) | 0.5094 (2) | 0.02174 (14) | 0.0206 (9) |
| 04 | 2/3 | 0.6456 (3) | 1/12 | 0.033 (2) |
| 05 | 0.7236 (3) | 0.4351 (3) | -0.02693 (13) | 0.0218 (10) |
| O6 | 0.3796 (3) | 1/3 | 1/12 | 0.0274 (15) |
| 07 | 0.5044 (3) | 0.3582 (3) | 0.02134 (14) | 0.0230 (10) |
| 08 | 0.5434 (3) | 0.4648 (3) | 0.09429 (14) | 0.0230 (10) |
| OW1 | 1.0336 (4) | 0.8092 (4) | 0.0328 (2) | 0.069 (2) |
| OW2 | 0 | 0 | $3 / 4$ | 0.164 (11) |

Table 2. Selected bond lengths $(\AA)$

| As1-08 | 1.772 (4) | V3-O1 | 1.605 (4) |
| :---: | :---: | :---: | :---: |
| As 1-07 | 1.778 (4) | V3-O3 | 1.926 (4) |
| As]-06 | 1.793 (3) | V3-O5 | 1.928 (4) |
| VI-O4 | 1.615 (6) | V3-O7 ${ }^{\text {II }}$ | 1.977 (4) |
| VI-O3 | 1.915 (4) | V3-08 ${ }^{\prime}$ | 1.989 (4) |
| $\mathrm{VI}-\mathrm{O}^{\prime}$ | $1.915(4)$ | K...OWl | 2.676 (6) |
| VI-O8' | 2.009 (4) | $\mathrm{K} \cdot \cdots \mathrm{O} 2^{11}$ | 2.768 (5) |
| V1--O8 | 2.009 (4) | K...O4 ${ }^{\text { }}$ | 2.805 (5) |
| $\mathrm{V} 2-\mathrm{O} 2$ | 1.604 (4) | K...O1 | 2.809 (5) |
| $\mathrm{V} 2-\mathrm{O} 5$ | 1.910 (4) | K. . OWI ${ }^{1}$ | 2.820 (7) |
| $\mathrm{V} 2-\mathrm{O} 5^{\text {ii }}$ | 1.939 (4) | K...O1'" | 2.847 (5) |
| $\mathrm{V} 2-\mathrm{O} 3$ | 1.955 (4) | K. . Of ${ }^{\text {¹1 }}$ | 3.311 (4) |
| V2-07 | 2.004 (4) |  |  |
| Symmetry codes: (i) $\frac{4}{3}-x, \frac{2}{3}-x+y, \frac{1}{6}-z$; (ii) $1-y, x-y, z$; (iii) |  |  |  |
| $1-x+y, 1-x, z ;$ (iv) $\frac{2}{3}+y, \frac{1}{3}+x,-\frac{1}{6}-z ;$ (v) $1+x-y, x,-z$; (vi) |  |  |  |
| $y, 1-x$ | $+x-y$ | $y,-\frac{1}{6}-z$. |  |

The highest peak in the difference map is $0.737 \AA$ from O8, and the largest hole is $0.931 \AA$ from OW1. The structure was refined by full-matrix least-squares techniques, using SHELXL93 (Sheldrick, 1993). All non-H atoms were assigned anisotropic displacement parameters in the refinement.
Data collection: XSCANS (Siemens, 1994). Cell refinement: XSCANS. Data reduction: SHELXTL-Plus (Sheldrick, 1990b). Program(s) used to solve structure: SHELXS86 (Sheldrick, 1990a). Program(s) used to refine structure: SHELXL93 (Sheldrick, 1993). Molecular graphics: SHELXTL-Plus. Software used to prepare material for publication: SHELXTLPlus.

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Supplementary data for this paper are available from the IUCr electronic archives (Reference: TA1192). Services for accessing these data are described at the back of the journal.

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# Inversion Symmetry in the Spin-Peierls Compound $\alpha^{\prime}-\mathrm{NaV}_{2} \mathrm{O}_{5}$ 

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#### Abstract

At room temperature, sodium pentaoxodivanadate, $\mathrm{NaV}_{2} \mathrm{O}_{5}$, was found to have the centrosymmetric space group Pmmn. This space group implies the presence


of only one kind of V site, in contrast with previous reports [Carpy \& Galy (1975). Acta Cryst. B31, 14811483] of the non-centrosymmetric $P 2{ }_{1} m n$ counterpart. This indicates a non-integer valence state of vanadium. Furthermore, this symmetry has consequences for the interpretation of the transition at 34 K , which was ascribed to a spin-Peierls transition of one-dimensional chains of $\mathrm{V}^{4+}$ ions.

## Comment

In recent years, low-dimensional quantum systems have revealed many new properties in their magnetic and electronic transport behavior. In many respects, the vanadates complement the copper oxide systems, with spinless $S=0, \frac{1}{2}$ and 1 states, obtained by $\mathrm{V}^{5+}\left(d^{0}\right)$, $\mathrm{V}^{4+}\left(d^{1}\right)$ and $\mathrm{V}^{3+}\left(d^{2}\right)$, or $\mathrm{Cu}^{+}\left(d^{10}\right), \mathrm{Cu}^{2+}\left(d^{9}\right)$ and $\mathrm{Cu}^{3+}\left(d^{8}\right)$, respectively. Recently, the first observation (Hase et al., 1993) of a spin-Peierls (SP) transition in an inorganic compound, $\mathrm{CuGeO}_{3}$, was complemented by the observation (Isobe \& Ueda, 1996) of an SP transition in $\mathrm{NaV}_{2} \mathrm{O}_{5}$. Evidence for this one-dimensional magnetic behavior was found in the temperature dependence of the susceptibility, which can be accurately described at high temperatures by the Bonner-Fisher (Bonner \& Fisher, 1964) model for an $S=\frac{1}{2}$ linear chain. Below $T_{\mathrm{SP}}=34 \mathrm{~K}$, an isotropic exponential decrease in the magnetic susceptibility is observed, evidence for a nonmagnetic ground state. The magnetic behavior of the SP state is complemented by SP signatures in a number of other measurements.

The usual interpretation of the transition at 34 K as a spin-Peierls transition is based on the structure determination of Carpy \& Galy (1975). Their refinement, based on photographic data, in the non-centrosymmetric space group $P 2{ }_{1} m n$, allows for two V -atom positions in the asymmetric unit. These sites were interpreted with different valence states, i.e. $\mathrm{V}^{4+}$ and $\mathrm{V}^{5+}$. In their model, the resulting one-dimensional $S=\frac{1}{2} \mathrm{~V}^{4+}$ chain can cause the observed Bonner-Fisher-like temperature dependence in the magnetic susceptibility, and a spin-Peierls transition at low temperature. However, the reported structure determination of Carpy \& Galy (1975) yielded atomic coordinates with a pseudo-inversion center at ( $0.259,0.25,0.11$ ) (Le Page, 1987, 1988). Therefore, we have undertaken a structure redetermination to investigate the (centro)symmetry.

The structure can be constructed from double rows of edge-sharing pyramids, one facing up and the other down. These double rows are connected by pyramid corner-sharing, yielding a planar material. These planes are stacked with the $\mathrm{Na}^{+}$ions in the channels of the pyramids, as shown in Fig. 1. The eightfold coordination of sodium is somewhat more symmetric [with Na O distances of $2.4325(11)-2.6038(9) \AA$ ] than in the refinement of Carpy \& Galy (1975) (Na-O 2.43$2.90 \AA$ ). The structure of $\mathrm{NaV}_{2} \mathrm{O}_{5}$ it thus similar to that

